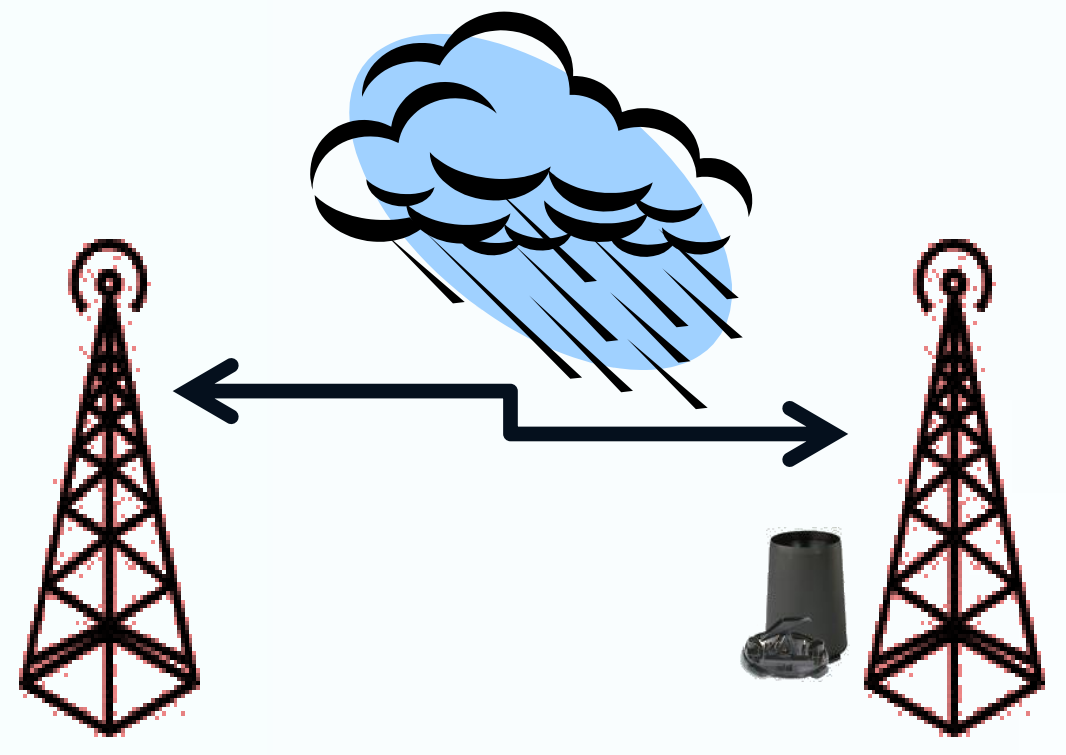


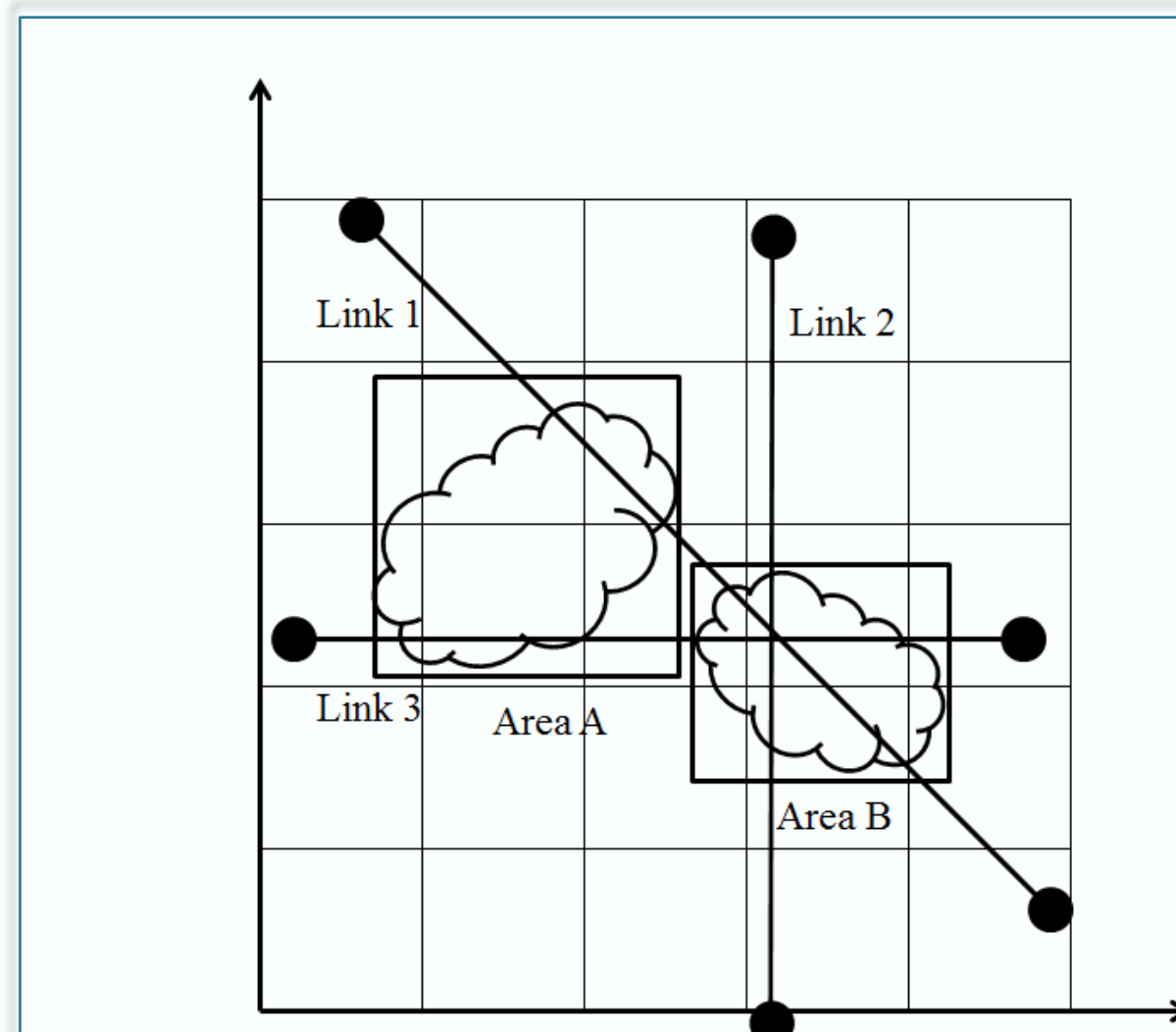
Compressed Sensing Based Detection of Localized Heavy Rain Using Microwave Network Attenuation

Gemalyn D. Abrajano, Takeshi Higashino and Minoru Okada
Graduate School of Information Science, Nara Institute of Science and Technology
{gemalyn-a, higa, mokada}@is.naist.jp

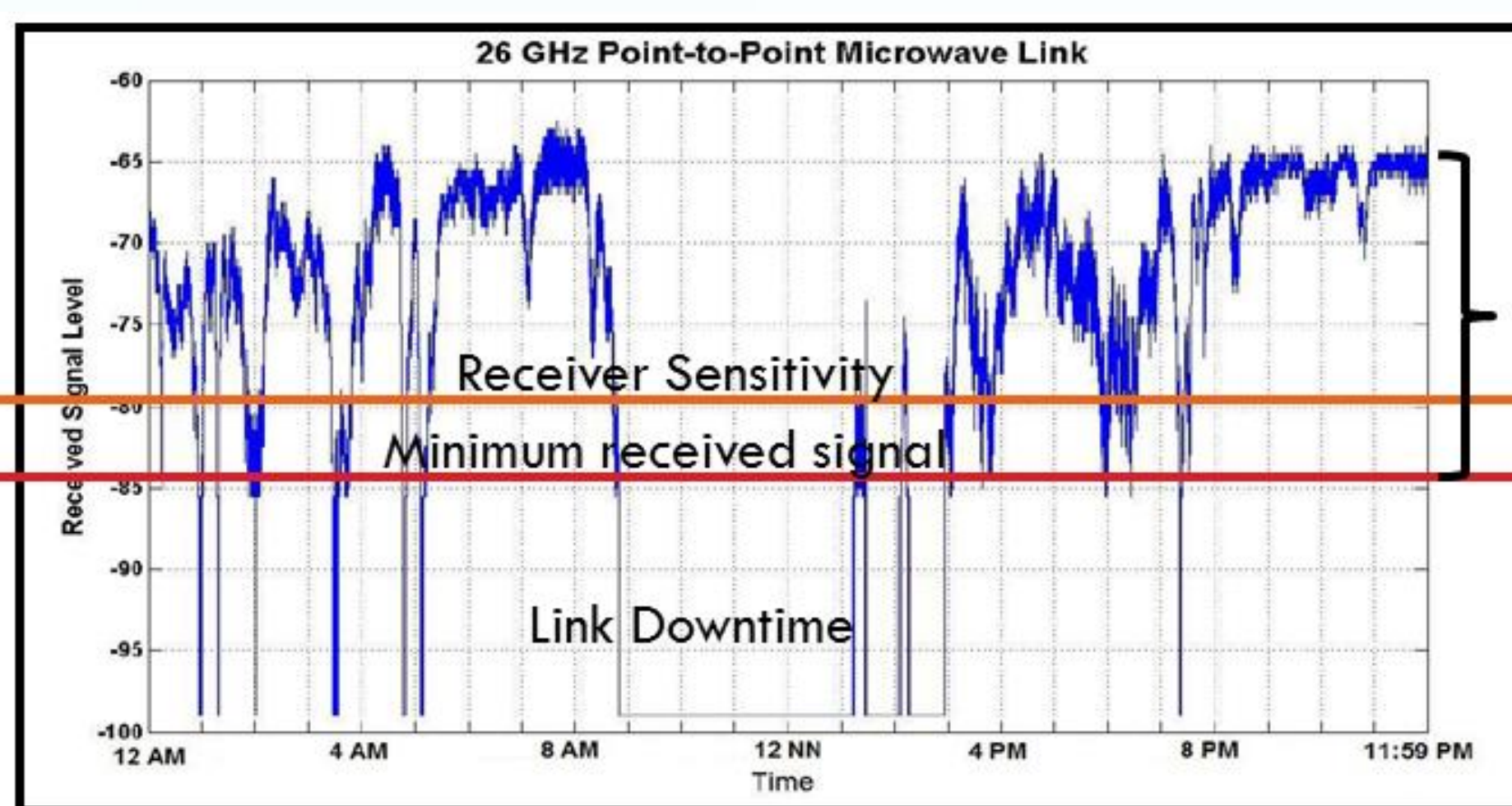
Microwave Mesh Network for Rain Detection



- The effective covered area of the links fit the size of rain clouds (less than 5 km)
- Already deployed as commercial links
- Designed to tolerate rain by a certain fade margin



- Microwave mesh network
- Each link's signal strength gets attenuated
- 1-2 links attenuated at the same time can indicate the rain location
- More crossing links - more accurate detection



Fade Margin

Objective:

To implement a compressed sensing-based method to detect localized heavy rain from the measured rainfall attenuation

Compressed Sensing Reconstruction

$$y = Ax$$

y : $M \times 1$
 A : $M \times N$ ($M < N$)
 x : $N \times 1$

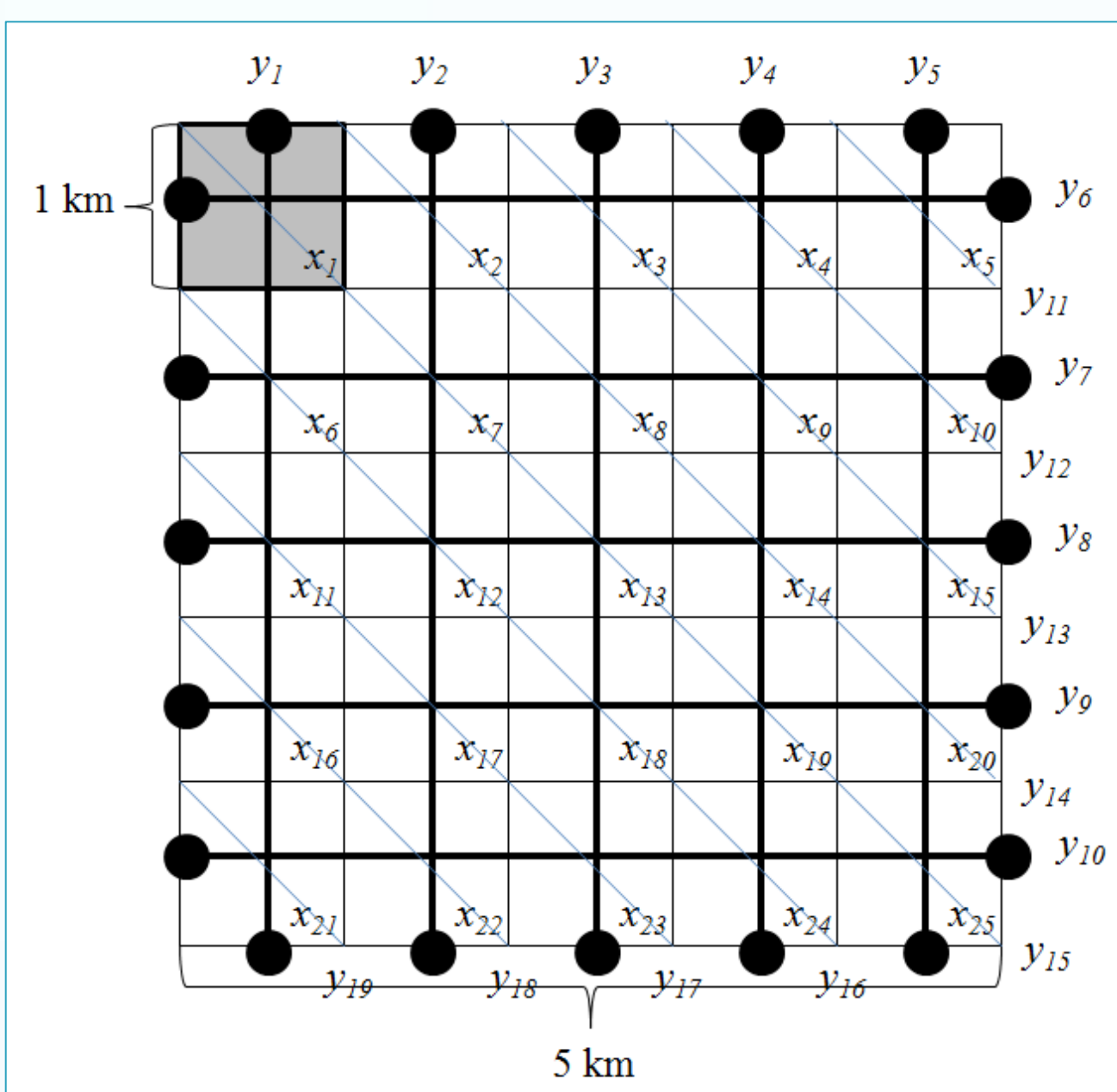
- measurements vector y
- measuring matrix A
- $y = Ax$, where x is sparse vector to be recovered

- Solution to underdetermined system through convex optimization (e.g. linear programming)

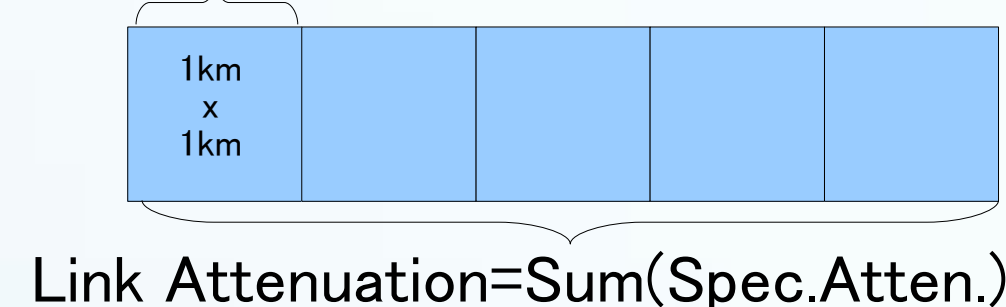
$$\hat{x} = \arg \min_x \|x\|_1$$

subject to $y = Ax$

Network Model



$$\text{Spec. Atten} = kR^\alpha$$



- 5km x 5km area in Okinawa
- Japan radar rain data (1km x 1km every 5 mins)
- 1 area $(x_1 - x_{25})$, 3 crossing links
- For 25 GHz, vertical polarization: (from ITU-R P.838.3)

$$k_v = 0.1533$$

$$\alpha_v = 0.9491$$

$$R = \text{rain rate}$$

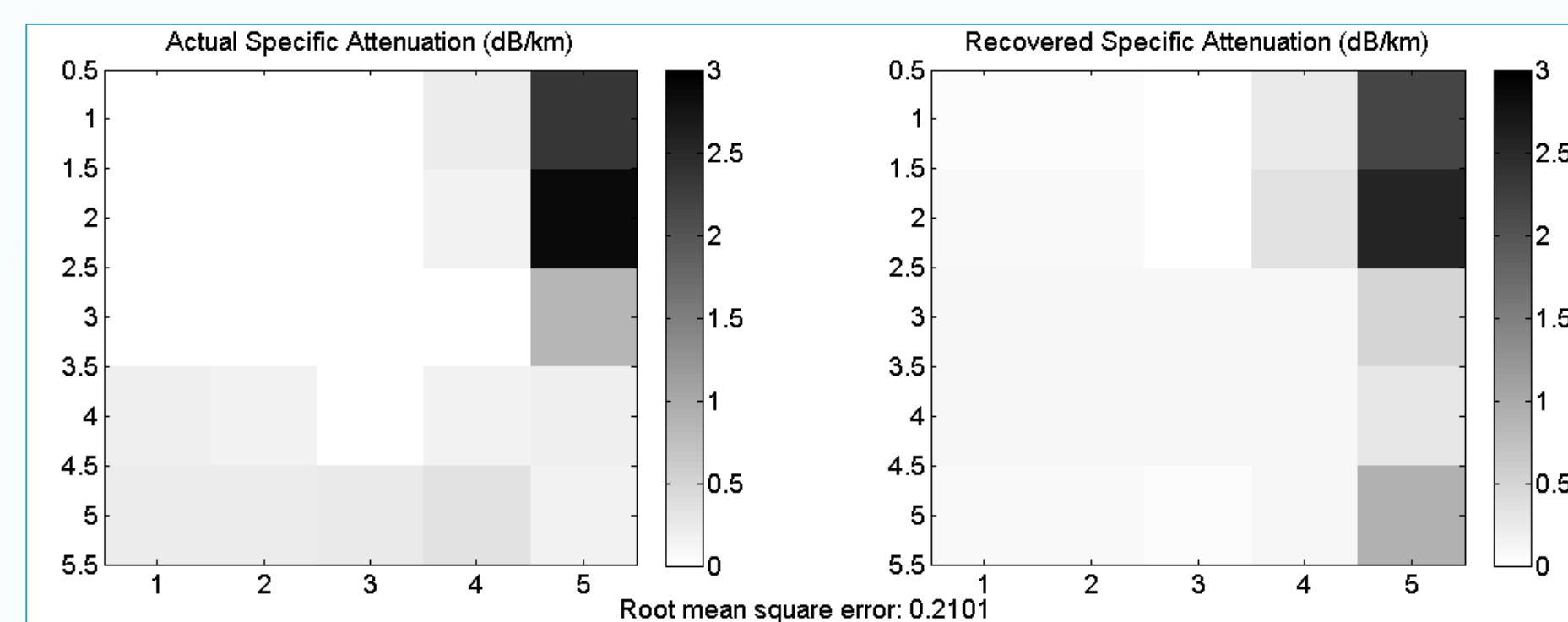
$$y_1 \dots y_{10} = \begin{bmatrix} \text{Link 1} & \text{Link 2} & \text{Link 3} \\ \text{Link 2} & \text{Link 1} & \text{Link 3} \\ \text{Link 3} & \text{Link 1} & \text{Link 2} \\ \dots & \dots & \dots \\ \text{Link 1} & \text{Link 2} & \text{Link 3} \end{bmatrix} x_1 \dots x_{25}$$

- y : link atten. measurements
- A : measurement matrix defined by areas with microwave links, where red and green are 1 and 0,
- x : unknown or the specific attenuation of a 1km x 1 km area

Results

Location Detection

- False positive rate: 4.03% (Out of 12733 samples, 45 were falsely marked moderate, 1 marked heavy, the rest light to negligible rain)
- False negative rate: $5.69 \times 10^{-5\%}$ or 18 data points



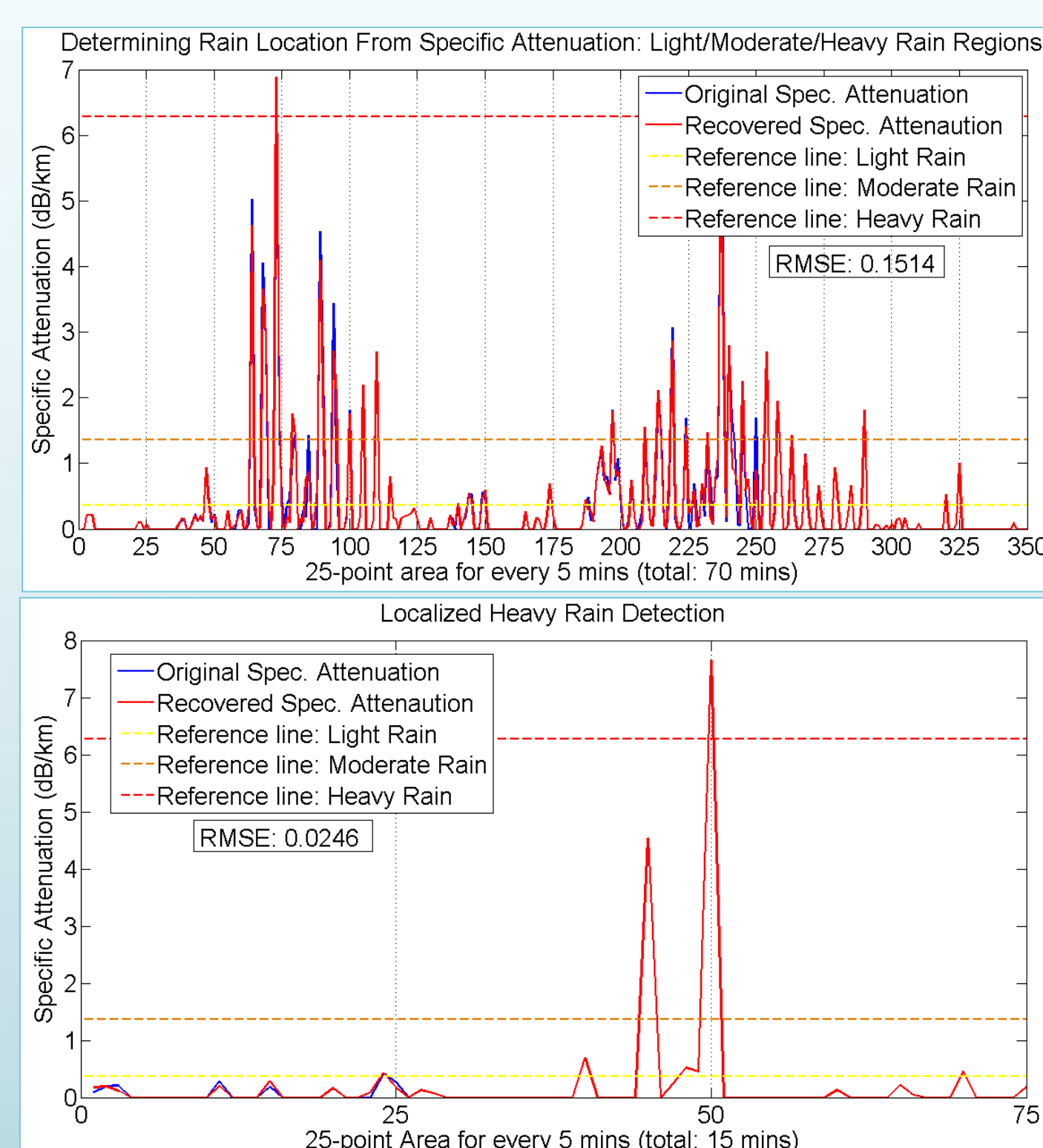
Recovered specific attenuation that causes high false positive rate

Rain Rate Detection

TABLE I. EVALUATION OF RECOVERED VALUES BASED ON RAIN RATE

Rain Rate (mm/hr)	Specific Attenuation (dB/km)	# of Data Points	RMS Error
No Rain	0	148,483	0.02
Light Rain	< 2.5	105,761	0.06
Moderate Rain	2.5 ~ 10	49,801	0.16
Heavy Rain	10 ~ 50	11,536	0.46
Violent Rain	> 50	544	1.27

- Errors are small and practically negligible
- Detection of heavy and violent rains are important

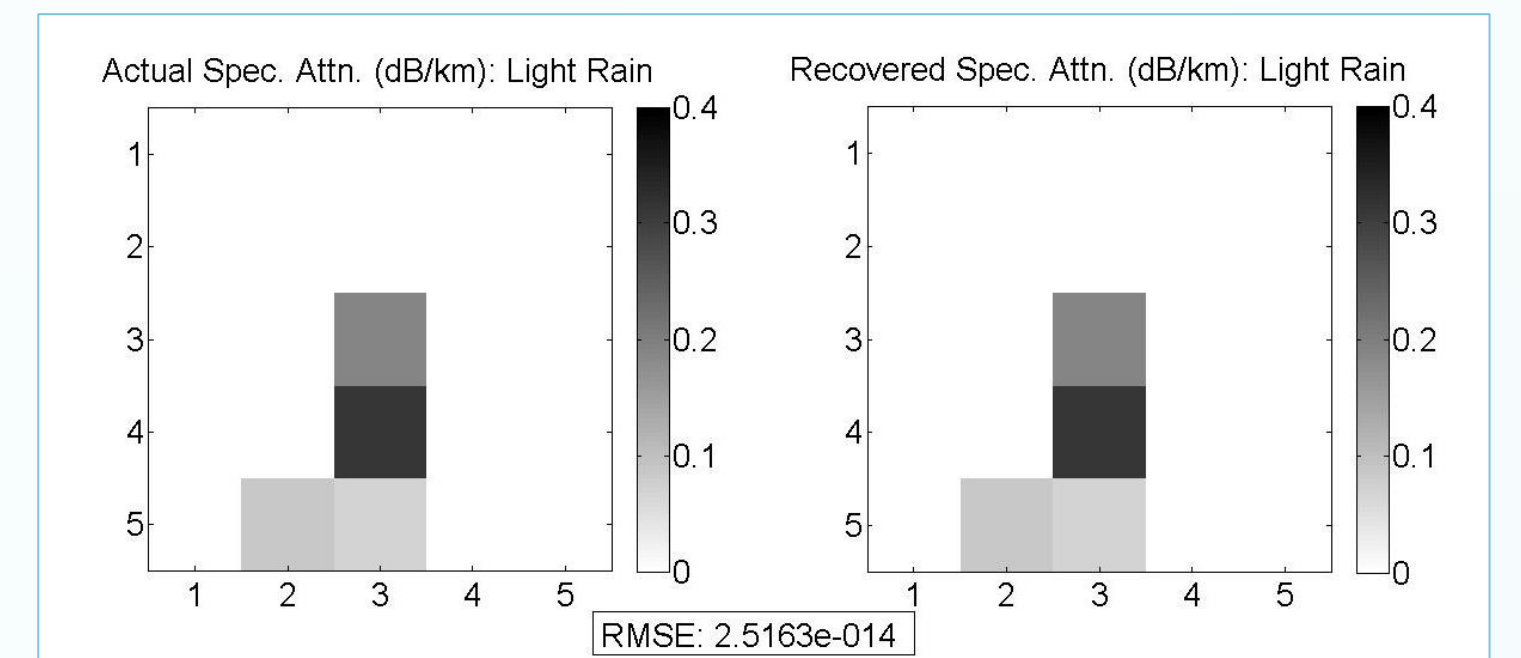


Horizontal axis: rainfall at p -th area out of 25-pt areas at time $5q$ -minute corresponds to index $Fp+25q$

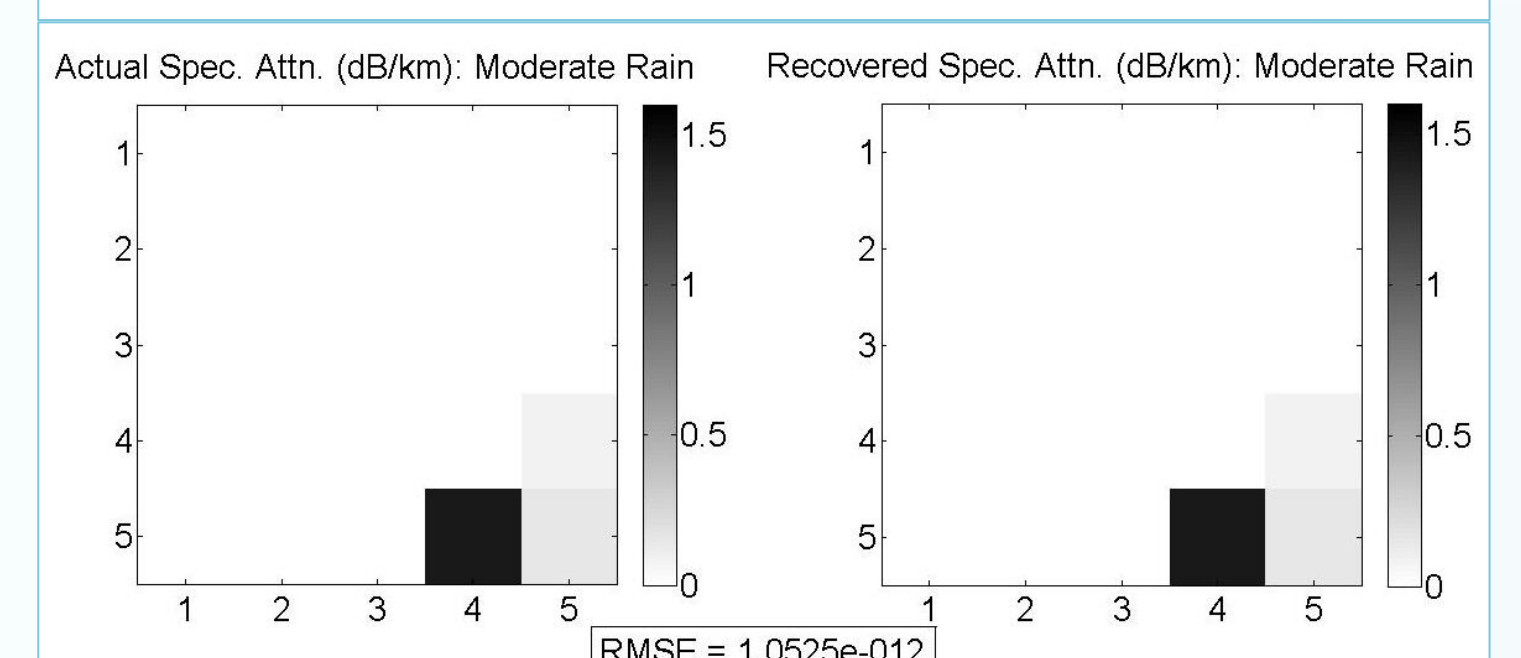
Rainfall Map

Reconstructions

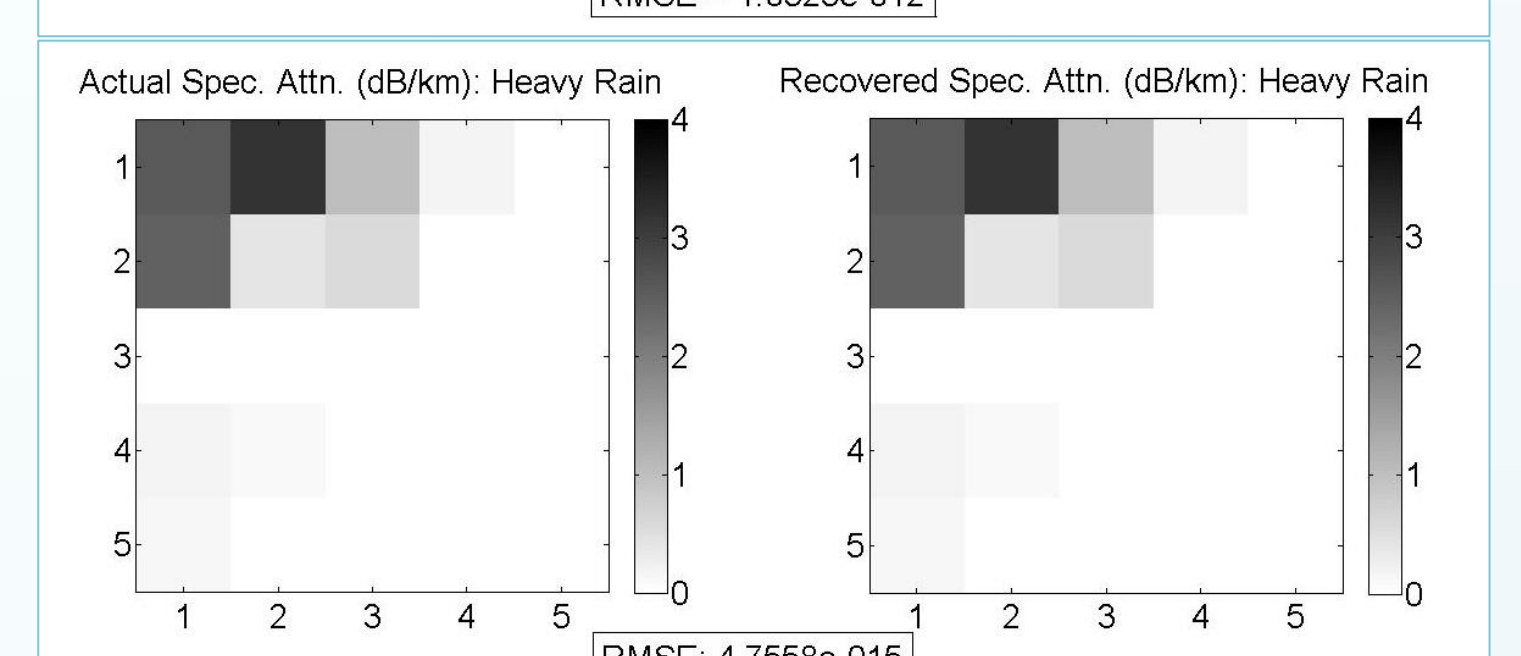
Light Rain



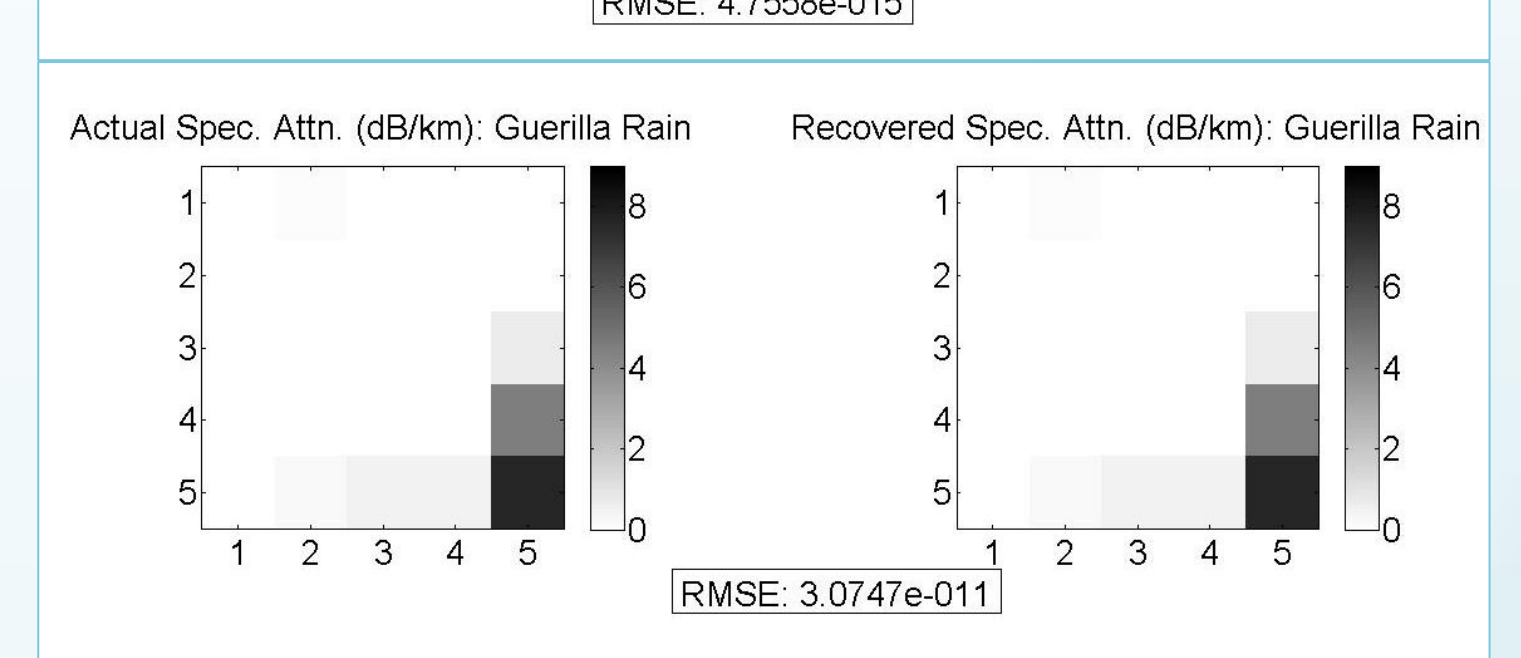
Moderate Rain



Heavy Rain



Localized Heavy Rain



Summary

- This research shows the reconstruction of the rainfall field from microwave attenuations using a compressed-sensing based algorithm.
- Proposed method works for all rain intensities, but works better for higher rain rates in smaller areas.
- Useful in the detection of localized heavy rain that can trigger disasters.
- Accuracy is improved when there are more links crossing a single area.
- Urban areas at risk with localized heavy rain will benefit from the proposed method because of the dense microwave networks deployed over them.